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PR

★ From "Single Screw Extruder Experiment" on Integrated Experience Website
$$Q = \left(\frac{n\pi R^3}{1+3m} \right) \left(\frac{\Delta P}{2mL} \right)^{\frac{1}{n}}$$

PROBLEMS BASED ON THE RHEOLOGY DEMO (SOME USING EXTRUDE2.XLS)

eq. 2 of extrusion manual

$$\Rightarrow \ln Q = \ln \left(\frac{n\pi R^3}{1+3m} \right) + \frac{1}{n} \ln \left(\frac{\Delta P}{L} \right) + \frac{1}{n} \ln \left(\frac{R}{2m} \right)$$

- (1) Using your data for flow rate Q vs. pressure drop, compute (at constant temperature) the power law parameters m and n for the HDPE at this temperature. Employ linear regression, working with the correct relation between Q and ΔP. Compute the viscosities from the ratios of shear stress and shear rate (at the wall). Follow the instructions in the spreadsheet for how to perform the linear regression.

$$\Rightarrow \ln Q = \ln \left(\frac{n\pi R^3}{1+3m} \right) + \frac{1}{n} \ln \frac{\Delta P}{L} + \frac{1}{n} \ln \frac{1}{m}$$

- (2) Note that I have used the equations derived in class to compute the shear rate in two different ways, both of which should give almost the same result. What are the 2 equations? Try to compare the viscosity or m,n data from either the *Polymer Handbook* or the *Encyclopedia of Polymer Science and Technology* (under "Olefin Polymers"). Both may be found in the reference section of Middleton Library, and elsewhere.

Plot $\ln Q$ vs. $\ln \frac{\Delta P}{L}$.

slope = $\frac{1}{n}$

Now you know n. Then intercept = $\ln \left(\frac{n\pi R^3}{1+3m} \right) + \frac{1}{n} \ln \frac{1}{m}$.

- (3) Assuming that the initial slope of the Q vs. RPM curve is correct, determine the % slippage or leakage of the extruder at higher Q's. This should increase with shear rate. Also examine your extrudate diameter data. Assuming the primary or first normal stress coefficient ψ varies similar to viscosity itself, and the die swell is directly proportional to ψ , what should be the functional relationship between die swell and shear rate?

Insert the known n and solve for m.

- (4) Estimate the temperature rise in the die at the wall assuming C_p for HDPE is 2300 J/(kg·K). Remember, the relevant volume is cylindrical. The actual temperature rise would only be about 20% of this number. Why?

I guess.....
 $Power = \eta \dot{\gamma}^2$
 $Power \cdot time = Work = C_p \Delta T$

$$\text{So } \Delta T = \frac{Power \cdot time}{C_p} = \frac{(\eta \dot{\gamma}^2) \left(\frac{L \pi R^2}{Q} \right)}{C_p}$$

- (5) Recent work on extrusion and injection molding has shown that the magnitude of die swell (extrusion) or warpage (injection molding) is affected by the material of the die or mold. In particular, very smooth, polished surfaces tend to give less swell. List some possible reasons for this phenomenon.

I'll guess 20% less due to acceleration of plug.

- (6) What are the chief rheological differences between Hair Conditioner (a suspension of PEG-100, PEG-5, PVA, PVP, guar, lecithin, long-chain alcohols, some cationic surfactants (quats), and some other low MW materials) and vinyl-terminated PDMS, as suggested by their behavior under oscillatory shear? How might some of the rheological properties of the Hair Conditioner contribute to its successful use? What about for the PDMS? NOTE: PDMS is used as biomedical implants, as heat transfer fluids, and as a component in personal care products such as body lotions.

In general terms, we expect relatively greater loss modulus (more phase lag in sinusoidal shear) for things that lack great physical extent (entanglements).

I dunno, but $\dot{\gamma} = \tau/\eta$

and $\dot{\gamma} = \left(\frac{Power}{\eta} \right)^{1/2}$

where Power

The energy dissipation rate, which Dr. Pooley sometimes calls Q, not to be confused with

volumetric flow rate.

We split this out as another problem.

X not graded